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Article

The CLoTH Simulator for HTLC Payment Networks with Introductory Lightning Network Performance Results

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Abstract: The Lightning Network (LN) is one of the most promising off-chain scaling solutions for Bitcoin, as it enables off-chain payments which are not subject to the well-known blockchain scalability limit. In this work, we introduce CLoTH, a simulator for HTLC payment networks (of which LN is the best working example). It simulates input-defined payments on an input-defined HTLC network and produces performance measures in terms of payment-related statistics (such as time to complete payments and probability of payment failure). CLoTH helps to predict issues and obstacles that might emerge in the development stages of an HTLC payment network and to estimate the effects of an optimisation action before deploying it. We conducted simulations on a recent snapshot of the HTLC payment network of LN. These simulations allowed us to identify network and payments configurations for which a payment is more likely to fail than to succeed. We proposed viable solutions to avoid such configurations.

Keywords: lightning network; payment channel; payment network; HTLC; simulator; blockchain; blockchain scalability; bitcoin

1. Introduction

Bitcoin is a decentralised cryptocurrency that allows mistrusting peers to send/receive monetary value without the need for intermediaries [1]. Bitcoin relies on the blockchain, a distributed peer-to-peer public ledger where each peer stores all the history of Bitcoin economic transactions. Its distributed and replicated nature along with a limited block dimension entails capped transaction throughput [2]. As proven in the comprehensive study by Gervais et al. [3], although more recent blockchains introduced technical solutions to reduce its extent, a commonly accepted blockchain design that resolves the scalability issue is not yet known.

One of the more explored technical proposals that addresses the blockchain scalability issue is the *off-chain scaling* [4–10], which enables off-chain payments, i.e., payments that do not need to be registered on the blockchain. Off-chain scaling approaches are based on *payment channels*. A payment channel is a two-party ledger which is updated off-chain and uses the underlying blockchain only as a settlement or dispute resolution layer. It allows an unbounded number of off-chain payments to be sent/received between two involved parties (the channel endpoints), as long as they can jointly reach consensus.

Two-party payment channels can be linked together to build a *payment network* for off-chain payments. This allows parties not directly connected by a payment channel to send/receive off-chain payments which are routed across a network of linked payment channels.

The *Lightning Network* (LN) [4] is the most developed off-chain solution and the mainstream payment network for Bitcoin. The LN protocol leverages a particular contract called *Hashed Timelock Contract* (HTLC) to build the payment network. The HTLC scheme allows transferring off-chain payments through multiple payment channels linked together. It guarantees transfer atomicity: even if a payment is carried across multiple intermediate channels to reach the recipient, the payment either succeeds or fails in all the involved channels. Henceforth, we define the *HTLC payment network* as a network of linked payment channels where payments are transferred using the HTLC scheme.

At its current state of development, the LN protocol is characterised by features that, if not properly understood, implemented and controlled, might undermine the development of a healthy HTLC payment network, i.e., a network that supports fast and successful payments. The features that need to be studied are the following: (1) source routing, i.e., a good routing path that does not cause a payment failure depends on the knowledge of an up-to-date network topology; (2) channel capacity, which constrains the payment amount; (3) channel unbalancing, namely, the condition of a skewed channel that has one endpoint depleted due to a number of unidirectional payments (an issue not internally addressed by the LN protocol); and (4) uncooperative behaviour of peers involved in a payment route, which increases payment time.

To avoid that these factors prevent the correct functioning of the HTLC payment network, also one of the more accredited LN development group claims the importance of protocol improvements and optimisation actions: in particular, the developers envision the need for special routing nodes, which are always online and contribute enough capital to route payments [11]. However, since the LN protocol design aims at ensuring systemic censorship resistance, the resulting lack of central coordination does not allow to predict outcomes of specific network configurations and/or optimisations.

In this work we present CLoTH, an HTLC payment network simulator. CLoTH simulator is a tool: to predict issues and obstacles that might emerge in development stages of an HTLC payment network; to assist in planning uncoordinated development of the network; to estimate the effects of an optimisation action before deploying it; to predict the return on investment of adding a hub to the network.

Examples of questions (expressed in simple English words) that can be answered by CLoTH are: (1) “How many channels per peer are required to have a robustly connected network?”; (2) “Which is the impact on performances of peers going offline?”; (3) “In which way payment amounts influence the probability of payment failures?”; (4) “How the mean payment time decreases by adding a peer with a specific set of payment channels in a specific point of the network?”.

The main contributions of our research are:

- The CLoTH simulator. It is a discrete-event simulator that simulates payments on HTLC payment networks. It takes as input parameters defining an HTLC network (e.g., number of peers and number of channels per peer) and parameters of the payments to be simulated on the defined HTLC network (e.g., the payment rate and payment amounts). It generates performance measures in the form of payment statistics, e.g., the probability of payment failure and the mean payment complete time. To the best of our knowledge, CLoTH is the first available simulator of HTLC payment networks.
- Simulation results produced using a recent snapshot of the HTLC payment network of LN. Such simulations allowed us to discover interesting cases when a payment is more likely to fail than to succeed on such network. Two such cases are the following: (1) when we set the payment rate to 100 payments per second, the network experienced 56.12% probability of payment failure; and (2) when we simulated payment amounts whose order of magnitude is between 1 millisatoshi and 0.0001 BTC (being worth less than \$1 at the time of writing), the network experienced 53.87% probability of payment failure.

Other contributions of our research are additional simulation runs on synthetic HTLC networks (i.e., HTLC payment networks generated by the simulator using their statistical description).

The results of these simulations show that: almost all synthetic networks have good performance (nearly 99% probability of payment success); if a network has 100 thousands peers, at least five channels per peers are required to have a well-connected decentralised network.

The remainder of the paper is organised as follows. Section 2 is a background on Bitcoin, off-chain scaling solutions and the Lightning Network. In Section 3, we describe the LN code we used as reference to develop the simulator. In Section 4, we present in detail the CLoTH simulator. In Section 5, we explain the design of the simulations we conducted. In Section 6, we show and discuss the results of the simulations. Finally, in Section 7, we provide conclusions and some possible future work.

2. Background

In this Section, we briefly explain the main concepts constituting the background of our research: Bitcoin and the blockchain; off-chain scaling solutions; and the Lightning Network.

2.1. Bitcoin and the Blockchain

Bitcoin is a decentralised payment system running on a peer-to-peer network. Transactions are used to transfer bitcoin cryptocurrency and they are defined by an input state and an output state. The output is represented by the amount of currency to be transferred and by a Bitcoin script defining the spending conditions to claim that amount. The input is represented by the reference to an output of a previous transaction and the proof fulfilling the spending conditions of the referenced output. The blockchain is the distributed ledger technology storing all Bitcoin transactions. Each peer (that runs a full node) stores a whole copy of the ledger. Miners are special peers that can write on the ledger: (i) they validate transactions broadcast on the peer-to-peer network against the ledger in order to prevent double spending of coins; and (ii) they gather transactions and write on the ledger, by broadcasting a block (i.e., a collection of transactions), ideally once every 10 min. For more details on Bitcoin and the blockchain, we refer the reader to the detailed background study by Bonneau et al. [12].

The Bitcoin blockchain is affected by a well-known scalability problem. Each block, in fact, has bounded size which imposes a limit to the transaction throughput. Such limit, on the one hand, contains the cost of storing the blockchain and validating and transmitting transactions [13], but, on the other hand, with a block size limit of 1 MB, the maximum transaction throughput is capped at around only seven transactions per second [14].

2.2. Off-Chain Scaling Approaches

Off-chain scaling approaches pursue scalability by moving off-blockchain as many transactions as possible.

2.2.1. Payment Channels

Payment channels [15] are the building block of the off-chain protocols. Such channels are implemented as two-party ledgers that allow two parties (the channel endpoints) to update their balances off-chain, without the limit imposed to blockchain transactions. The blockchain is used only as a dispute resolution layer when and if consensus about the off-chain state cannot be reached off-chain between channel endpoints.

In the rest of this section, we leverage the following example of a payment channel.

Payment channel example. Alice and Berto open a payment channel. Alice funds the channel with 0.5 BTC, Berto funds the channel with 0.5 BTC, so Alice's initial *balance* in the channel is 0.5 BTC and Berto's is 0.5 BTC. The *capacity* of the channel is the total amount of bitcoins in the channels: 1 BTC. After opening the channel, Alice can transfer 0.1 BTC off-chain to Berto: to do so, they update accordingly their balances in the channel, thus Alice's balance is 0.4 BTC and Berto's balance is 0.6 BTC. Channels are bidirectional, so also Berto can pay Alice. It is important to notice that no transactions on

the blockchain are required to accomplish these payments between Alice and Berto: they just update their bidirectional off-chain balances.

2.2.2. Payment Network

A payment network is a network of payment channels linked together, to avoid that every possible pair of peers has to open bidirectional payment channels for off-chain payments. With respect to blockchain transactions, off-chain payments performed in payment networks are: cheaper, as lower fees are required to route payments in such networks; faster, as they do not need to be registered on the blockchain; and more privacy preserving, as they are not visible in the public blockchain.

In the rest of the section, we leverage the following example of a payment network.

Payment network example. Alice sends 0.1 BTC off-chain to Davide, without having a direct payment channel with him. She exploits a route of already open channels linking her to Davide: the channel she has with Berto; the channel between Berto and Carola; and the channel between Carola and Davide. To find this route of payment channels, source routing is applied: it is Alice who has to find which intermediary hops her payment needs to go through.

2.3. The Lightning Network

The Lightning Network (LN) is the mainstream implementation of a network of payment channels for Bitcoin. It was introduced in 2015 by Joseph Poon and Thaddeus Dryja [4].

2.3.1. LN Payment Channel Lifecycle

The payment channel lifecycle, as specified by the LN protocol, is presented in the following.

Channel funding. Alice and Berto create a *funding transaction*, the transaction required to fund the channel. The funding transaction is broadcast to the blockchain and, when confirmed, the channel is considered open. Alice and Berto create also a *commitment transaction*, which represents their respective current balances in the channel: such transaction spends the bitcoins in the funding transaction and transfers 0.5 BTC to Alice and 0.5 BTC to Berto. The commitment transaction is *not* broadcast to the blockchain.

Payment execution. When Alice wants to pay 0.1 BTC to Berto, the two parties create a new commitment transaction which reflects the new balances: 0.4 BTC of Alice and 0.6 BTC of Berto. No transaction is sent to the blockchain, i.e., the operation is done off-chain.

Channel closing. When the two parties want to close the channel, they send the last updated commitment transaction to the blockchain.

Punishments to disincentivise misbehavior. Berto can punish Alice if Alice misbehaves (or vice versa), thanks to the *Revocable Sequence Maturity Contract* (RSMC), a contract implemented by a script in the spending condition of the commitment transaction. Alice could be tempted to broadcast an old commitment to the blockchain, for instance, the commitment preceding her payment to Berto, when she owned more funds (0.5 against 0.4 BTC). If Alice tries to do so and Berto notices the old commitment transaction in the blockchain, Berto can take all the funds of the channel (even the 0.4 BTC of Alice's balance), by broadcasting the last commitment transaction with the RSMC to the blockchain. Therefore, since Alice may lose all her funds, she is disincentivised to misbehave.

Channel unbalancing. A channel is said unbalanced or skewed when one balance is much higher than the other. If payments always flow from Alice to Berto and no payments flow from Berto to Alice, Alice's balance may go to zero. Channel unbalancing constitutes a problem, as a payment cannot traverse a channel in a given direction if the balance in that direction is lower than the payment amount.

2.3.2. Hashed Timelock Contract (HTLC)

HTLC is a contract for off-chain multi-hop payment through channels that connect the payment sender and the payment recipient. An off-chain multi-hop payment is the atomic composition of several off-chain payments, each one performed on an intermediate payment channel. An intermediate peer receives an inbound payment on one of its channels and forwards the same amount to the next payment hop (actually a little less since it retains a small fee for intermediary service), until the payment arrives to the recipient. In this way, the HTLC scheme creates a network of payment channels along which off-chain payments can be routed.

In practice, the HTLC contract is implemented by a script in the spending condition of the commitment transaction of a payment channel and it executes conditional payments. Alice pays 0.1 BTC to Berto if Berto can demonstrate to know a value R within a certain timeout (*timelock*, in the Bitcoin jargon): in this case, the HTLC is fulfilled; otherwise, 0.1 BTC returns back to Alice and the HTLC fails. Funds in the HTLC payment stay locked up to the disclosure of R or, if R is never disclosed, up to the timelock expiration. In the following, we describe the phases of a payment from Alice to Davide using HTLCs.

HTLC establishment. For the multi-hop payment originated by Alice and trying to reach Davide, the following HTLCs are established: (1) the HTLC between Alice and Berto, where Alice pays 0.1 BTC to Berto if Berto demonstrates to know R within a certain timelock, e.g., three days; (2) the HTLC between Berto and Carola, where Berto pays 0.1 BTC to Carola if Carola demonstrates to know R within two days; and (3) the HTLC between Carola and Davide, where Carola pays 0.1 BTC to Davide if Davide demonstrates to know R within one day.

HTLC fulfillment. Alice sends R to Davide, and HTLCs from Davide to Alice are fulfilled: Davide shows R to Carola within one day, and Carola pays him 0.1 BTC; Carola shows R to Berto within two days, and Berto pays her 0.1 BTC; Berto shows R to Alice within three days, and Alice pays him 0.1 BTC. At the end, 0.1 BTC has been transferred from Alice to Davide. For their work of forwarding the payment, Berto and Carola can withhold a small fee when transferring the payment (which, for simplicity, we omitted in this example). It is important to highlight that all the described operations are performed off-chain, without the need to interact with the blockchain. Finally, it is worth noticing that, from Davide to Alice, HTLCs have increasing timelocks. This ensures that each party has enough time to know R and claim her funds: Davide shows R to Carola in one day, Carola pays 0.1 BTC to Davide; after that, Carola still has one day to claim 0.1 BTC from Berto, as the timelock with Berto is set to two days.

HTLC failure. If R is not disclosed by an uncooperative peer, the payment fails in all channels. A failure message is sent back to Alice and no payment occurs between the channels, as HTLC conditions have not been fulfilled. In addition, in such case, funds in the HTLC stay locked up to the timelock expiration. If Davide does not disclose R , Carola has to wait one day to get back 0.1 BTC according to the HTLC conditions. After that, Carola closes the channel with Davide by broadcasting the last commitment transaction to the blockchain and propagates back the failure to Alice.

2.4. Brief Literature

Although the most developed, the Lightning Network is not the only off-chain payment network in the literature.

Christian Decker presented Duplex Micropayment Channels for building an off-chain payment network based on HTLCs [5]. With respect to this approach, the key novelty of LN is the possibility of punishing a misbehaving party in the channel.

Raiden [7] uses smart contracts to implement the same fundamental concepts of LN in the Ethereum blockchain.

Sprites [6] is an attempt to improve both LN and Raiden, as it aims at minimising the time during which funds are locked while being transferred via HTLCs.

3. Preliminary Analysis

For implementation level details of HTLC mechanisms, we took as reference 1nd, the Golang implementation of the Lightning Network. 1nd, as the other LN implementations (e.g., c-lightning [16], and eclair [17]), fully conforms to the so-called *Basis of Lightning Technology* (BOLT) [18], the Lightning Network specifications.

In Figure 1, we show the multi-hop payment call graph resulting from our analysis of commit 65dede2 of the 1nd public GitHub repository (while for our implementation we used commit 4d6cd2e, a more recent commit in which function `findPaths` has been replaced by a blacklist-based routing described below). The call graph represents the functions called when a payment flows from a sender to a receiver through an intermediate hop. These functions implement the HTLC mechanism that ensures the atomicity of the payment (cf. Section 2.3.2).

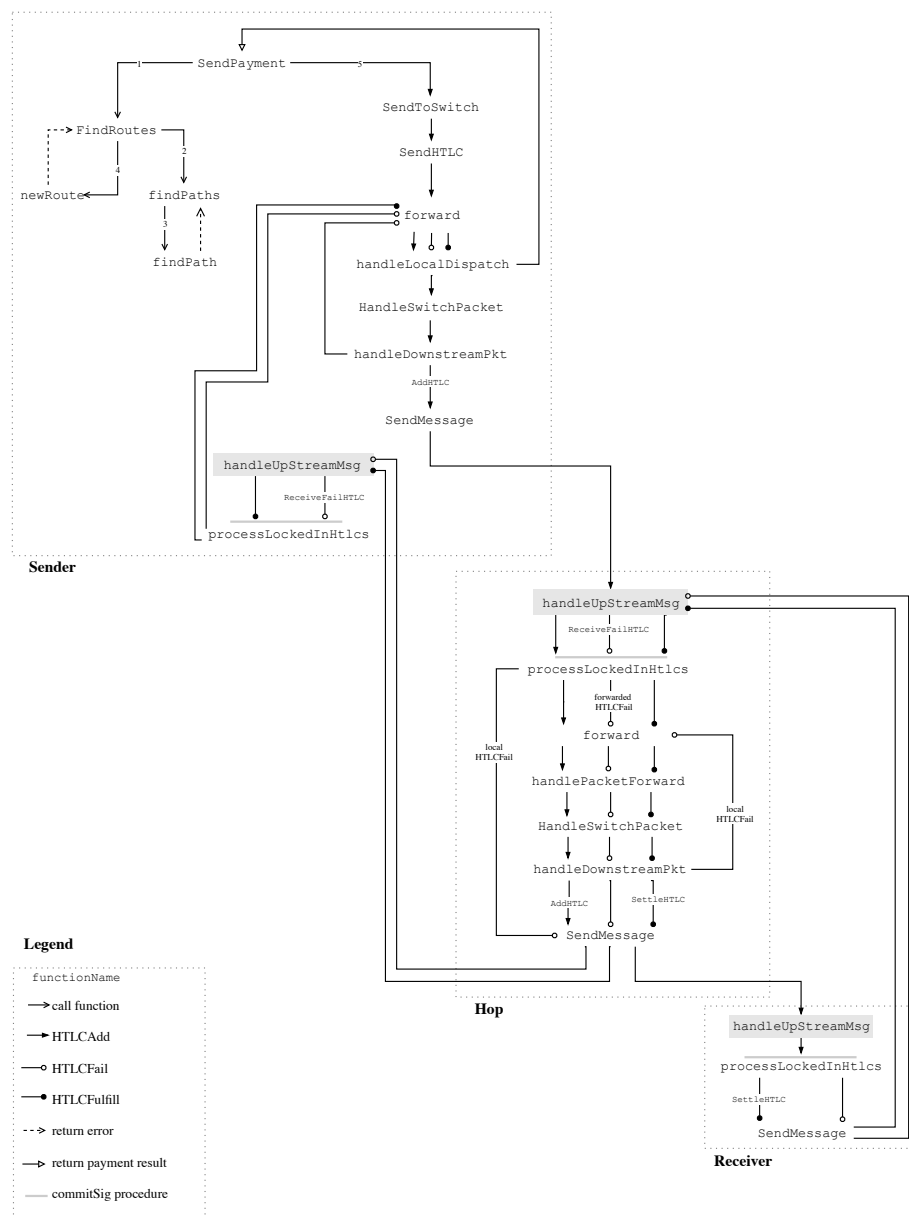


Figure 1. Multi-hop payment call graph of 1nd.

We depict three peers, as they call different functions with different behaviours: the payment sender \mathcal{S} , the payment receiver \mathcal{R} and a generic intermediate hop \mathcal{H} . This case can be easily generalised to the n -intermediaries one since the behaviour of each intermediate hop is always the same.

HTLC messages (i.e., HTLCAdd, HTLCFulfill and HTLCFail) that flow through peers are represented by arrows:

- HTLCAdd: sent from \mathcal{S} to \mathcal{R} through \mathcal{H} , for the establishment of HTLCs among the peers;
- HTLCFulfill: sent from \mathcal{R} to \mathcal{S} through \mathcal{H} , for the fulfillment of the HTLCs; and
- HTLCFail: sent in case of failures, for failing the HTLCs.

The function `handleUpStreamMsg` in the gray box represents the first function called by a peer when an HTLC message is received. The gray line represents the `commitSig` procedure that establishes an HTLC: the creation of a new commitment transaction containing the HTLC between the two involved parties.

In Appendix A, we describe the details of the 1nd code and of the functions of the call graph, while in the following we provide an high-level description of the flow of a payment.

Payment initialisation and sending. Source routing is run by \mathcal{S} to search for an available route to \mathcal{R} . If no route is found, the payment is considered failed; otherwise, \mathcal{S} sends an HTLCAdd message to \mathcal{H} to establish the HTLC.

Payment relay (intermediate hop). \mathcal{H} checks for possible errors (e.g., it checks whether it has enough balance to forward the payment). If there are errors, it sends an HTLCFail message back to \mathcal{S} , failing the HTLC; otherwise, it sends an HTLCAdd message to \mathcal{R} . (This step occurs multiple times in the general case of a payment going through multiple intermediate hops.)

Payment reception. \mathcal{R} checks for possible errors. If there are errors, it sends an HTLCFail message to \mathcal{H} (which in turn propagates it to \mathcal{S}), failing the HTLCs; otherwise, it sends an HTLCFulfill message to \mathcal{H} (which in turn propagates it to \mathcal{S}), for fulfilling the HTLCs.

Payment re-attempt. If an HTLCFail is received by \mathcal{S} , \mathcal{S} tries to re-attempt the payment by searching for a new route. If the failure was due to a channel which did not have enough balance to forward the payment, the channel is blacklisted. If the failure, instead, was due to an uncooperative peer, the peer is blacklisted. A new route is looked for excluding peers and channels in the blacklist. If no new route is found, the payment is considered definitively failed.

4. Simulator Design

In this Section, we provide a detailed description of the CLoTH simulator, which is, to the best of our knowledge, the first simulator for HTLC payment networks. By HTLC payment network, we mean a network where peers are connected by payment channels and off-chain payments are routed using HTLC contracts.

The simulator takes as input the definition of an HTLC network and the payment script to be played during the simulation. It simulates payments in the HTLC network by locally running a discrete-event mapping of the 1nd code. It produces performance measures in the form of payment-related statistics (e.g., the probability of payment failures and the mean payment complete time).

4.1. Assumptions

An HTLC payment network relies on a blockchain as a securing mechanism for all the payment channels which form the network. The underlying blockchain is therefore a fundamental prerequisite of each HTLC payment network. We assume channels are loaded with an amount of native tokens from the underlying blockchain and fees for payment forwarding are due to the intermediary hops in the same denomination.

CLoTH does not consider blockchain interactions during a simulation execution, since the performance measures produced by the simulator are related to payments, which are completely performed off-chain. Simulations run on a network in which no new channels are opened. This condition is implicitly guaranteed if the whole simulation time is shorter than the time required to accumulate a large enough number of confirmations for funding a new channel with an on-chain transaction. For this reason, we made each simulation last about 15 min, since to deem a transaction as definitive on Bitcoin it is usual to wait for six confirmations (about 60 min). Without loss of generality, we do not take into account those channels that might have been established early enough before the simulation starting time to become operative during the simulation time window.

Another assumption we made in the simulator is that each peer has a complete and precise knowledge of all other peers and channels in the network. In reality, as specified in BOLT, new channels and peers are announced through a gossip protocol. Therefore, real performance may result slightly worse than the one measured by CLoTH, as in reality peers may have a slightly imprecise knowledge of the network, due to imperfections of the gossip protocol.

4.2. Software Architecture

CLoTH is a *discrete-event* simulator [19]. Events represent state changes of the simulated system. The *event loop* is the core of the simulation engine: it extracts the next event from a queue where events are sorted according to their occurring time; it advances the simulation time to the instant of occurrence of the event being currently processed; and it calls the function that processes the event.

The simulator generates an event each time a payment changes its state according to the state diagram in Figure 2. Each type of event in the diagram is processed by a function of the same name of the simulator, as explained in the following Section.

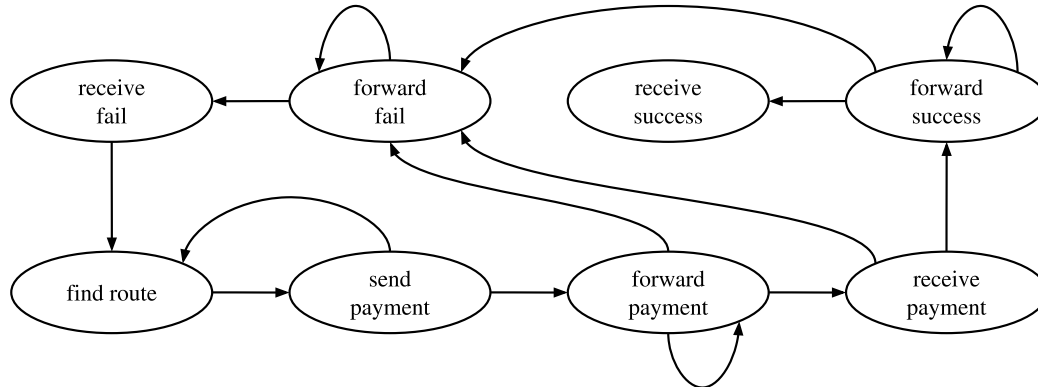


Figure 2. CLoTH simulator events state diagram.

4.2.1. Computation Flow

Table 1 shows the mapping between each function of the 1st computation flow and functions of the CLoTH simulator codebase. The completeness of the mapping ensures the validity of the simulated results.

Table 1. Mapping between CLoTH simulator functions and 1nd functions.

Simulator Function	Description	Simulated Functions	Peer	Message
find_route	Search for a payment route	SendPayment, FindRoutes, findPath, newRoute	Sender	-
send_payment	Send a payment	SendToSwitch, SendHTLC, forward, handleLocalDispatch, HandleSwitchPacket, handleDownstreamPkt, AddHTLC, SendMessage	Sender	HTLCAdd
forward_payment	Forward a payment	handleUpstreamMsg, processLockedInHtlcs, forward, handlePacketForward, HandleSwitchPacket, handleDownstreamPkt, AddHTLC, SendMessage	Hop	HTLCAdd
receive_payment	Receive a payment	handleUpstreamMsg, processLockedInHtlcs, SendMessage, SettleHTLC	Receiver	HTLCAdd
forward_success	Forward the successful result of a payment	handleUpstreamMsg, processLockedInHtlcs, forward, handlePacketForward, HandleSwitchPacket, handleDownstreamPkt, SettleHTLC, SendMessage	Hop	HTLCFulfill
forward_fail	Forward the fail result of a payment	handleUpstreamMsg, processLockedInHtlcs, forward, handlePacketForward, HandleSwitchPacket, handleDownstreamPkt, ReceiveFailHTLC, SendMessage	Hop	HTLCFail
receive_success	Receive the successful result of a payment	handleUpstreamMsg, processLockedInHtlcs, forward, handleLocalDispatch	Sender	HTLCFulfill
receive_fail	Receive the fail result of a payment	handleUpstreamMsg, processLockedInHtlcs, forward, handleLocalDispatch, ReceiveFailHTLC	Sender	HTLCFail

Table 1 makes a clear distinction between particular behaviours of each 1nd function which depends on two parameters: (1) the type of peer that invokes it (i.e., sender, receiver or intermediate hop); and (2) the type of the triggering message (HTLCAdd, HTLCFail, HTLCFulfill). For example, the function `send_payment` of the simulator simulates the functions `SendToSwitch`, `SendHTLC`, `forward`, `handleLocalDispatch`, `HandleSwitchPacket`, `handleDownstreamPkt`, `AddHTLC` and `SendMessage` of the 1nd code, when they are called by the payment sender in the case of HTLCAdd message.

Uncooperative behaviour. Functions `forward_payment`, `receive_payment` and `forward_success` simulate the uncooperative behaviour of a peer. Using Bernoulli probability distributions, we determine whether a peer is uncooperative and, if so, whether it is uncooperative after or before establishing the HTLC. If the peer is cooperative, the function is normally executed. If the peer is uncooperative before establishing the HTLC, as specified by the LN protocol, an HTLCFail is propagated back to the payment sender and the payment is re-attempted with a new route that does not encompass the uncooperative peer. Finally, if the peer is uncooperative after establishing the HTLC, as specified by the LN protocol, an HTLCFail is propagated back to the payment sender after the timelock expiration and the channel connecting to the uncooperative peer is closed. Then, the sender can re-attempt the payment, with a new route excluding the closed channel.

4.2.2. Data Structures

Figure 3 shows main attributes of the simulator data structures. A channel connects two peer (each one represented by an ID) and has a certain capacity. The endpoint of a channel describes how a peer behaves in a specific channel and contains: the current balance of the endpoint in that channel; base and proportional fee, which constitute the fee withheld by the endpoint for forwarding a payment (proportional fee is the part of the fee which depends on the payment amount, while base fee is the constant fee applied regardless of the payment amount); and the timelock set in the HTLCs established by the channel endpoint. A payment is described by a sender, a receiver and the payment amount.

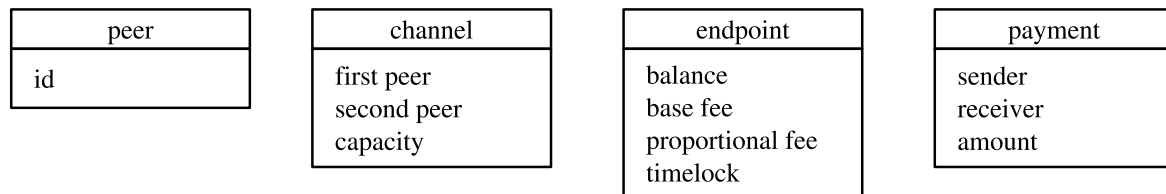


Figure 3. CLoTH simulator data structures.

4.3. Workflow and Usability

The workflow to interact with the CLoTH simulator is shown in Figure 4. It is composed by three phases: (1) pre-processing phase; (2) simulation phase; and (3) post-processing phase. For the sake of clarity, we first introduce the simulation phase. Then, the explanations of the pre-processing and post-processing phases follow.

4.3.1. Simulation Phase

Input attributes. The simulation engine requires two inputs:

1. A complete specification of the HTLC network (Files 3, 4 and 5 in Figure 4). These files allow for a fine grained specification of the attributes of Figure 3 of peers (`peers.csv`), channels (`channels.csv`) and endpoints (`endpoints.csv`).
2. The detailed list of payments to be executed with their attributes (File 6 in Figure 4, `payments.csv`), specifying sender, receiver, payment amount and triggering time.

Although verbose, this input specification allows for the most detailed definition of the simulation scenario. For a succinct and statistically meaningful input configuration mode, the reader can resort to the pre-processing phase of the workflow described below.

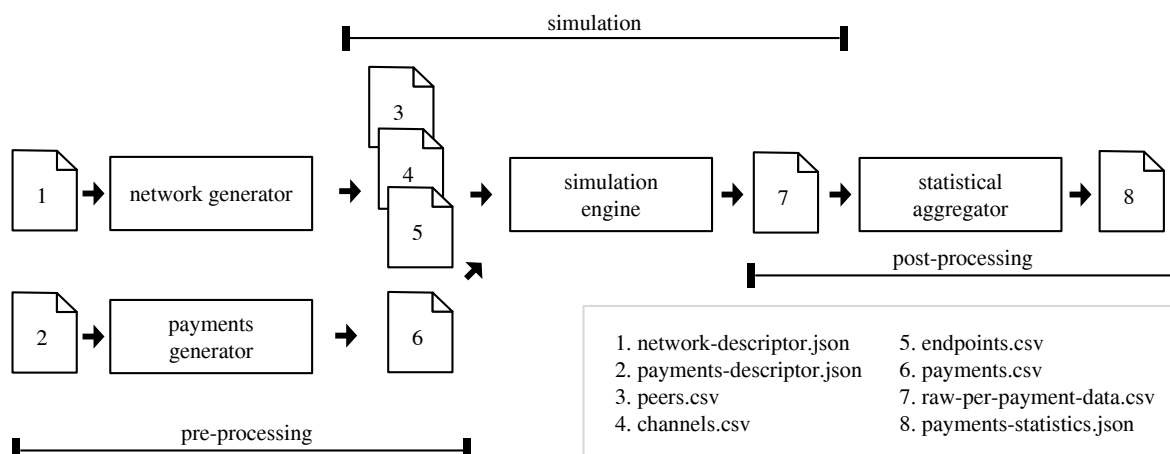


Figure 4. CLoTH simulator workflow.

Simulation engine execution. Given the HTLC network and the payments specified as input, the simulation engine executes the payments on the HTLC network, running the actual discrete-event simulation.

Output attributes. The simulation phase outputs detailed information about each simulated payment (File 7 in Figure 4, `raw-per-payment-data.csv`):

- the end instant of the payment;
- the result of the payment: success or failure;
- the number of times the payment was attempted;
- whether the payment encountered an uncooperative peer; and
- the route traversed by the payment, if present.

4.3.2. Pre-Processing Phase

We wanted the CLoTH simulator to support fine-grained simulations as well as the possibility to concisely describe a simulation from a statistical point of view. While the input described in Section 4.3.1 directly supports the first case, the second requirement is fulfilled by the pre-processing phase. This phase takes as input a few parameters that statistically characterise both the network and the payments to be simulated. Then, it randomly generates an instance of HTLC network and an instance of payment script that match the input description.

Input parameters. Input parameters of the pre-processing phase with their symbols are shown in Table 2. The following parameters deserve an explanation:

- σ_t tunes the presence of hubs in the network topology. It is the width of the Gaussian distribution which defines the probability of connection among peers. In particular, for each peer, this Gaussian probability distribution is used for choosing the other endpoint of one of the peer channels. Therefore, if the width of this Gaussian is zero, all peers have one channel open with the same peer, which, consequently, will be an hub. On the contrary, if the Gaussian width is infinite, any peer has the same probability to be connected to any other, thus producing a totally decentralised network.
- σ_a tunes payment amounts. It is the width of the Gaussian distribution whose tail is used to choose the orders of magnitude of payment amounts. The greater this width is, the longer the Gaussian tail is, and the higher the payment amounts.
- F_{sr} is the fraction of the total payments directed toward the same recipient. Such parameter allows modelling the use case of many small payments sent to the same destination peer, e.g., to a provider of video-streaming services which is paid for each short segment of video streaming.

Table 2. CLoTH simulator pre-processing phase input parameters.

Type	Symbol	Definition
Network	N_p	Number of peers
	N_{ch}	Average number of channels per peer
	σ_t	Tuner of network topology
	$P_{\bar{c}_b}$	Uncooperative peers probability before HTLC establishment
	$P_{\bar{c}_a}$	Uncooperative peers probability after HTLC establishment
	C_{ch}	Average channel capacity
	G	Gini index of channel capacity
Payments	r_π	Average payment rate
	N_π	Number of payments
	σ_a	Tuner of payment amounts
	F_{sr}	Fraction of same-recipient payments

4.3.3. Post-Processing Phase

The post-processing phase transforms raw per-payment simulation output attributes into statistically meaningful performance measures (File 8 in Figure 4, `payments-statistics.json`). To do so, it applies the *batch means* method [19], which allows: (i) producing performance results that are not influenced by the initial transient state, where the system is not stable; and (ii) computing statistical mean, variance and 95% confidence interval for each measure. The batch means method consists in dividing a simulation run into multiple batches, which are statistically independent among each other. Output measures are zeroed and re-computed at each batch. Each final output measure is the statistical mean of that measure over the batches and comes also with variance and 95% confidence interval.

Simulation results format. The performance measures produced by the simulator are shown in Table 3 with their symbols. Some clarifications are presented in the following:

- P_{fr} is the probability that a payment fails due to the absence of a route connecting sender and receiver.
- P_{fb} is the probability that a payment fails because a channel in the route was unbalanced and an alternative route is not found.
- P_{fc} is the probability that a payment fails because a peer in the route was uncooperative and an alternative route is not found.
- $P_{\bar{k}}$ represents the remaining fraction of payments for which we do not know whether they failed or succeeded, as they ended after the time validity window of our simulation. For example, this category can encompass payments delayed after a long timelock, as a peer was uncooperative after establishing the HTLC for the payment.
- T is the mean time for a successful payment to complete.
- N_a is the mean number of times a payment is re-attempted.
- L_r is the mean route length traversed by a successful payment.

Table 3. CLoTH simulator performance measures.

Symbol	Definition
P_s	Probability of payment success
P_{fr}	Probability of payment failure for no route
P_{fb}	Probability of payment failure for unbalancing
P_{fc}	Probability of payment failure for uncooperative peers
$P_{\bar{k}}$	Probability of unknown payments
T	Payment complete time
N_a	Number of payment attempts
L_r	Payment route length

4.4. Formal Model

Having a network with N nodes connected by payment channels and having M payments to be executed on this network, the simulator formal model can be expressed using the following formulas:

$$r_k = \phi(p_k, \mathcal{G}_k, b_k) \quad (1)$$

$$\mathcal{G}_{k+1} = \mu(p_k, r_k) \quad (2)$$

Function ϕ is the function which finds a route for a payment. It takes as input the following parameters:

- $p_k = (n_{i_k}, n_{j_k}, a_k)$ for $k = 1, 2, \dots, M$ is the payment for which a route has to be found: n_{i_k} and n_{j_k} are the sender node and the receiver node of the payment, for $i, j = 1, 2, \dots, N$ and $i \neq j$; and a_k is the payment amount.

- \mathcal{G}_k is the graph of nodes n_i for $i = 1, 2, \dots, N$ connected by payment channels. The subscript k indicates the state of the graph at the moment in which p_k is processed, with the available nodes and channels and their attributes at that moment.
- b_k is the blacklist of possible nodes and channels excluded when searching for a route for p_k (cf. Section 3).

The output r_k is the route found for the payment p_k .

Given the payment p_k and the route r_k , function μ executes the payment p_k along the route r_k . Such function produces a new state of the graph, namely \mathcal{G}_{k+1} , because the payment execution causes some changes in the channels involved in the payment, such as the update of channel balances accordingly to the payment amount a_k .

4.5. Performance

Table 4 shows the performance of the CLoTH simulator in terms of execution time. Simulation times refer to experiments run on a machine of model DGX-1, manufactured by Nvidia, located in Rome, Italy. The machine is equipped with 80 CPUs of model Intel® Xeon® CPU E5-2698 v4 @ 2.20 GHz and 512 GB of RAM. Table 4a shows that execution time increases with the increase of the number of peers of the simulated network. This is due to the fact that time consumed by the Dijkstra's algorithm, used to find payment routes, grows with the number of peers. With 1 million peers, a simulation run requires more than four days.

Table 4. CLoTH simulator execution time: (a) as a function of the number of peers; and (b) as a function of the number of Dijkstra calls.

(a)	
Peers	Execution Time (h)
100,000	6.64
200,000	15.92
500,000	49.25
700,000	64.68
1,000,000	104.15
(b)	
Dijkstra Calls	Execution Time (h)
58,927	4.98
303,374	28.3

Table 4b shows that the execution time also increases with the increase of the number of calls to the Dijkstra's algorithm. An execution of the Dijkstra's algorithm is required each time a payment is attempted, so the more times the payments is re-attempted, the higher the number of calls to the Dijkstra's Algorithm is, and the higher the simulation execution time is. The execution of the Dijkstra's algorithm constitutes a bottleneck for the performances of the simulator. However, there are no limits on the values of the input parameters. The only effect of setting high values (e.g., an high number of peers or payments) is a correspondingly long execution time.

5. Simulation Experiments Design

In this Section, we present two groups of simulation experiments on HTLC payment networks:

1. Simulations on the LN mainnet. In this set of simulations, we gave as input to the simulator peers and channels taken from a recent snapshot (downloaded on 14 June 2018 at 14:32 from LN explorer [recksplorer](#)) of the Lightning Network running on top of the Bitcoin main network (called *mainnet*, in the Bitcoin jargon). The goal of this set of simulations was to discover the cases (if any) in which a payment is more likely to fail than to succeed on the LN mainnet.

2. Simulations on synthetic networks, i.e., HTLC networks generated by the network generator included in CLoTH (cf. Figure 4). The goal of these additional simulations was to study the impact of each individual input parameter on HTLC network performance. Therefore, this set of simulations took into account also the parameters defining the HTLC network, which were by definition fixed in the simulations of the LN mainnet.

The results of the study, i.e., performance measures under different network and payment configurations, are reported in Section 6.

5.1. Parameter Tuning

Each simulation experiment is defined by a set of independent variables. They are a subset of the simulator input parameters and attributes (input of pre-processing and simulation phases, respectively; cf. Section 4.3). The dependent variables are performance measures in the form of payment-related statistics, i.e., the output of the post-processing phase of the CLoTH simulator.

Variation Intervals

Each independent variable is studied in a proper *variation interval*. A variation interval is defined by its extreme values and by its sampling rate (i.e., the grain of its subdivisions, how many intermediate steps are considered). Table 5 shows the variation intervals for each independent variable.

Table 5. Variation intervals of the independent variables.

Variable	Interval	Unity of Measure
N_p	[100,000 200,000 500,000 700,000 1,000,000]	-
N_{ch}	[3 5 8 11]	-
σ_t	[0 1 10 inf]	-
$P_{\bar{c}_b}$	[0 0.01 0.1 1.0 10.0]	%
$P_{\bar{c}_a}$	[0.01]	%
C_{ch}	[100 1,000 10,000 100,000 1,000,000]	satoshi
G	[0.0 0.1 0.2 0.4 0.6 0.8]	-
r_π	[10 100 1000]	payments per second
N_π	[10,000 100,000 1,000,000]	-
σ_a	[1 2 3 4 5]	-
F_{sr}	[0 10 20 40 50]	%

Regarding the topology tuner σ_t , Figure 5 shows the images of the resulting topologies for each of the values of the variation interval. In this Figure, node size is directly proportional to the number of open channels of the node. It can be noticed that: with $\sigma_t = 0$, there is just one single big peer, which constitutes a centralised hub with many open channels; with $\sigma_t = inf$, instead, there are no hubs as all peers have the same size; and, with the middle values of σ_t , there are some scattered hubs.

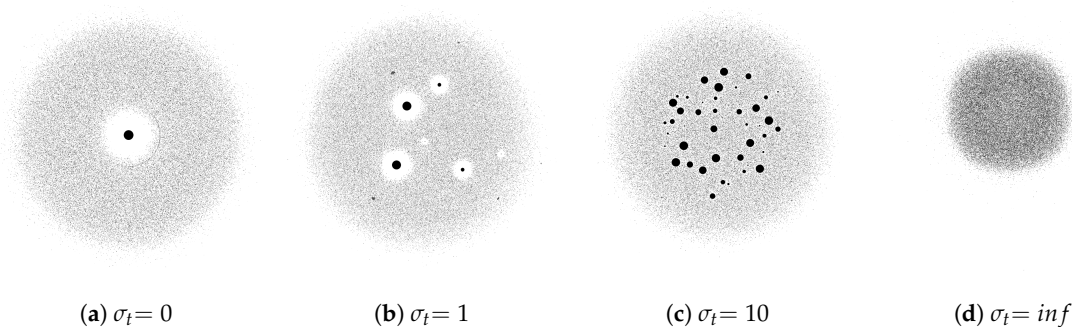


Figure 5. Resulting network topologies for different values of σ_t .

Regarding the payment amounts tuner σ_a , Table 6 shows, for each value of σ_a , the payment amounts generated, in the form of: order of magnitude expressed in satoshi and fraction of payments whose amount has that order of magnitude. These are the orders of magnitude used for the simulations on the LN mainnet, while for the simulations on synthetic networks we increased by two each order of magnitude: the LN mainnet, in fact, being in its early stage of adoption, can tolerate only small payment amounts.

Table 6. Percentage of payments with a certain order of magnitude for each value of σ_a .

Order of Magnitude (Satoshi)	σ_a				
	1	2	3	4	5
10^{-3}	67.83%	35.26%	26.33%	20.38%	18.00%
10^{-2}	27.61%	29.57%	23.76%	19.85%	17.43%
10^{-1}	4.3%	18.80%	18.40%	17.14%	15.53%
10^0	2.6%	8.81%	13.79%	13.88%	14.14%
10^1	0.0%	3.32%	8.80%	11.48%	11.49%
10^2	0.0%	0.98%	5.08%	8.19%	9.69%
10^3	0.0%	0.20%	2.58%	5.55%	8.19%
10^4	0.0%	0.06%	1.26%	3.53%	5.51%

We ran some initial tuning simulations to define the intervals of the independent variables. We provide the rationales of each variation interval in the following:

- Number of peers N_p . A network with fewer than 100 thousands peers is too small, since the LN is supposed to scale Bitcoin. Regarding the upper limit, as shown in Section 4.5, a simulation with 1 million peers lasts more than four days, which is incompatible with the time constraints of our research activities (to be addressed in future research).
- Average number of channels per peer N_{ch} . With the tuning simulations, we noticed that with fewer than three channels per peer all payments fail, since the network is not properly connected. With 11 channels per payments, instead, no payments fail for absence of route, so performance would not improve with more than 11 channels.
- Topology tuner σ_t . The two limits, infinite and zero, correspond to the two opposite cases: totally decentralised and one single hub, respectively. The values in between are used to generate networks with some scattered hubs.
- Uncooperative peers probability before HTLC establishment $P_{\bar{c}_b}$. Regarding the choice of the upper limit, we deemed that a probability that a peer is uncooperative more than once every 10 times is unrealistic.
- Uncooperative peer probability after HTLC establishment $P_{\bar{c}_a}$. Payments failing for such uncooperative peers are not captured by our simulation since they end after the simulated time interval (because of the timelock). However, it is realistic to have this value different from zero, as it may happen with a certain small probability that a peer experiences a fault and goes offline after establishing an HTLC.
- Channel capacity C_{ch} . A channel capacity lower than 100 satoshis (which corresponds to \$0.001 at writing time) would mean that the channel is unable to transfer anything but so-called dust payments. The upper limit is chosen in order to support the maximum payment amount and corresponds to one order of magnitude greater than such maximum.
- Gini index G . The Gini index is by definition a value between 0 and 1.
- Average payment rate r_π . A payment rate lower than 10 payments per second is not realistic for a world-wide payment system as LN aspires to be. The highest value is the average rate supported by mainstream traditional payment systems.
- Number of payments N_π . The values of this interval depend on the average payment per second, and on the fact that we force a simulation to last around 15 min (cf. Section 4.1).

- Payment amount tuner σ_a . The lowest value produces only small payments, but not lower than 1 millisatoshi (corresponding to 10^{-8} at writing time), to avoid dust payments (cf. Table 6). The highest value is to produce a certain fraction of high payments, however not higher than 0.001 BTC (less than \$10), as the Lightning Network at least at this stage is not supposed to support large payments.
- Fraction of same-recipient payments F_{sr} . We consider unrealistic to send to the same recipient more than half of the total payments during a single simulation.

5.2. Simulations on the LN Mainnet

In this category of simulations, we set the input of the simulator using a recent snapshot of the LN mainnet. The goal of such simulations is to discover *non-operative* cases, i.e., cases in which the network is non-operative. We define the network as non-operative when it is more likely for a payment to fail than to succeed.

The only independent variables in this set of simulations are the payment parameters and the probability of uncooperative peers, as the other parameters are determined by the LN mainnet. For each independent variable we define:

- *Non-stressing value*: A value of the variation interval which is *not* supposed to negatively impact performance. For example, the non-stressing value for the uncooperative peers probability is zero, as in this case all peers are cooperative and do not cause payment failures.
- *Stressing value*: A value of the variation interval which is supposed to negatively impact performance. For example, the stressing value for the probability of uncooperative peer is 10%, as it is the highest probability of uncooperative behaviour specified in the variation interval.

Table 7 shows the full list of stressing and non-stressing values for the independent variables of these simulations.

Table 7. Stressing and non-stressing values of independent variables.

Variable	Non-Stressing Value	Stressing Value
r_π	10	100
N_π	10,000	100,000
σ_a	1	5
F_{sr}	0%	50%
P_{c_b}	0%	10%

We adopted a branch-and-bound-like strategy to discover non-operative cases. The branch-and-bound tree of the simulations we ran is depicted in Figure 6. Each node represents a simulation, and the name of the node refers to the independent variable we stressed in that simulation. We proceeded in the following way:

- We started from the non-stressing simulation, where all variables are set to their respective non-stressing values.
- We stressed one individual independent variable at a time, thus forming a branch for each simulation with one stressed independent variable.
- If the simulation with the stressed variable produced a non-operative case, we stopped; otherwise, we continued examining that branch, stressing additional variables.

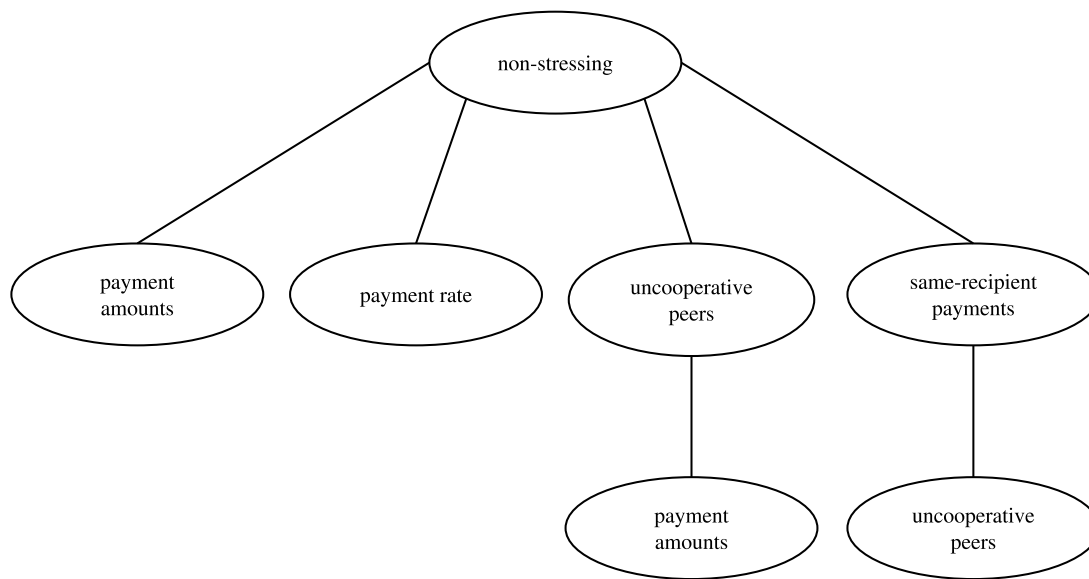


Figure 6. Branch-and-bound-like strategy for simulations on the LN mainnet.

The formal algorithmic description of such strategy is shown in Algorithm 1, where \mathcal{ST} represents the set of stressed independent variables and $P(\mathcal{ST})$ the probability of payment success resulting from the simulation with the stressed variables in \mathcal{ST} .

Algorithm 1 Branch-and-bound-like strategy.

```

1: for each independent variable  $v$  do
2:    $\mathcal{ST} \leftarrow v$ 
3:   for each independent variable  $u \neq v$  do
4:     if  $P(\mathcal{ST}) < 50\%$  then
5:       break
6:     else
7:        $\mathcal{ST} \leftarrow \mathcal{ST} + u$ 
8:     end if
9:   end for
10: end for

```

5.3. Simulations on Synthetic Networks

In this set of simulations, we study the effect on performance of one independent variable at a time. For each independent variable, we ran more simulations, one for each of its values in the variation interval. When studying a variable, the variables not under observation are set to a *default value*, i.e., a reasonable value in the interval for which that variable does not interfere with the results of the simulation. For example, for studying the effect of σ_t , we ran four simulations, one for each value of σ_t defined in the variation interval (cf. Table 5); in each one of the four simulations, the other independent variables were set to their respective default values.

We did not adopt the branch-and-bound-like methodology for finding non-operative cases of synthetic networks because the resulting computational load would be too high. In fact, with eleven input parameters, the branch-and-bound-like strategy would require a very high number of simulations. We will pursue this direction in future work.

In the following, we explain the rationale of the chosen default values (shown in Table 8).

- Number of peers N_p . We did not choose a higher value because of the limited maximum execution time of the simulator; however, we performed a set of simulations varying the number of peers in the variation interval, to show the results for different values of such variable.
- Number of channels per peer N_{ch} . We used the value suggested by the LN developers [20].
- Network topology tuner σ_t . The chosen value produces no hubs in the topology, since the LN, as Bitcoin, is supposed to work in a decentralised topology.
- Uncooperative peers probability $P_{\bar{c}_b}$ and $P_{\bar{c}_a}$. The chosen values represent a realistic probability that a peer goes down for a fault.
- Channel capacity C_{ch} . The chosen value is higher than the maximum payment amount we used in the simulations.
- Gini index G . The chosen value produces a uniform distribution of bitcoins in the channels. In this way, performance is not influenced by an unbalanced distribution of bitcoins, where some channels have an high capacity and the others have a low one.
- Average payment rate r_π . It was set to the middle of the variation interval, neither too high nor too low.
- Number of payments N_π . It depends on the average payment rate, to ensure that the simulation does not last more the maximum duration allowed (15 min).
- Payment amount tuner σ_a . It was set to the lowest level possible in our interval, to avoid the performance being influenced by high amount payments, when the effect of payment amount is not under observation.
- Fraction of same-recipient payments F_{sr} . It was set to zero to avoid that such payments influence the performance in simulations in which their effect is not under observation.

Table 8. Default values of independent variables.

Variable	Default Value
N_p	100,000
N_{ch}	5
σ_t	inf
$P_{\bar{c}_b}$	0%
$P_{\bar{c}_a}$	0.01%
C_{ch}	100,000
G	0.0
r_π	100
N_π	100,000
σ_a	1
F_{sr}	0%

6. Results and Discussion

In this Section, we present and discuss the results of both sets of simulations.

6.1. Simulations on the LN Mainnet

At the time of the snapshot, the LN mainnet presented the following features:

- Number of peers: 1221.
- Number of channels: 5167.
- Average degree (number of open channels per peer): 9.92.
- Average channel capacity: 381.35 satoshis.
- Gini index (concentration of bitcoins in channel capacities): 0.85.

As the reader can see, the LN mainnet is in its early development and adoption stage. It is small, as few peers and channels are present, and channel capacities are still low. Such premature state explains at least partially the non-operative cases found by our simulations.

We discuss the following simulations one branch at a time (cf. the branch-and-bound tree in Figure 6) to show the path we followed to discover non-operative cases. For each discussed branch, we show the results of the simulations corresponding to that branch, starting from the non-stressing simulation (the root of the tree), up to the last simulation in the branch (the leaf of the branch). The results of each simulation are presented in the following way: the values of the independent variables in that simulation, emphasizing the stressed ones; and the probability of payment success/failure that resulted from the simulation. The detailed results (which include all output measures) are available [online](#).

6.1.1. Branch: Payment Amounts

In these simulations, we study the effects of stressing payment amounts. We started from the non-stressing simulation and then we ran a simulation in which we stressed σ_a . The results are shown in Table 9.

Table 9. Simulation results of the branch of payment amounts.

Input Parameters				Output Measures			
r_π	σ_a	F_{sr}	$P_{\bar{c}_b}$	P_s	P_{f_r}	P_{f_b}	$P_{f_{\bar{e}}}$
10	1	0.0%	0.0%	65.43%	24.40%	10.11%	0.0%
10	5	0.0%	0.0%	46.13%	46.11%	7.72%	0.0%

We found a non-operative case, as with a stressed σ_a the probability of payment success turned out to be 46.13%, i.e., below 50%. Comparing the probabilities of payment failure between the non-stressing case and the amount-stressed case, we noticed an increase of the probability of payment failure for no route (46.11% against 24.40%), while the other probabilities of payment failure remain almost the same. This is due to the fact that capacities of channels are not enough to forward payments of higher amounts, thus a viable route for those payments is not found.

6.1.2. Branch: Payment Rate

In these simulations, we studied the effects of a stressed payment rate. Starting from the non-stressing simulation, we ran a simulation with a stressed payment rate (100 payments per second). The results are shown in Table 10.

Table 10. Simulation results of the branch of payment rate.

Input Parameters				Output Measures			
r_π	σ_a	F_{sr}	$P_{\bar{c}_b}$	P_s	P_{f_r}	P_{f_b}	$P_{f_{\bar{e}}}$
10	1	0.0%	0.0%	65.43%	24.40%	10.11%	0.0%
100	1	0.0%	0.0%	43.88%	25.17%	30.92%	0.0%

We discovered a non-operative case, as the stressed payment rate caused a probability of success of 43.88%. The cause is the increase of the probability of payment failure for unbalancing, which was around 20% higher with respect to the non-stressing simulation (30.92% against 10.11%). The reason of this result is that channel balances are depleted by the increased number of payments to be forwarded.

6.1.3. Branch: Same-Recipient Payments

In this branch, starting from the non-stressing condition, we firstly stressed the fraction of payments directed to the same recipient, set to half the total number of payments (5000 payments). The results in Table 11 show that such stress did not worsen performance. The probability of payment success increased with respect to the non-stressing simulation (69.45% against 64.43%). Such increase is

due to a decrease of the probability of payment failure for no route: from 24.4% to 18.81%. The reason for such behaviour is that the peer to which we directed half of payments has many open channels. Consequently, payments directed to this peer more probably found a viable route, with respect to the non-stressing case, in which payments were sent to different randomly-selected peers.

To make sure that we did not miss a non-operative case, we ran a further simulation stressing a second parameter. The only parameter we could stress was the probability of uncooperative peer. We could not, in fact, stress the payment amount, as the use case of payments directed to the same recipient is realistic only when such payments have low amount, and we could not stress the payment rate, since we already showed that with 100 payments every second the network was non-operative. The results of this simulation show that, with both F_{sr} and $P_{\bar{c}_b}$ stressed (the latter set to 10%), the HTLC network remains operative. With respect to the case of only F_{sr} stressed, the probability of failures for uncooperative peers increased to 14.84%, however, the probability of success is above 50% (57.1%), therefore the network resulted operative in this case too.

Table 11. Simulations results of the branch of same-recipient payments.

Input Parameters				Output Measures			
r_π	σ_a	F_{sr}	$P_{\bar{c}_b}$	P_s	P_{f_r}	P_{f_b}	P_{f_e}
10	1	0.0%	0.0%	65.43%	24.40%	10.11%	0.0%
10	1	50%	0.0%	69.54%	18.81%	11.61%	0.0%
10	1	50%	10.0%	57.10%	18.80%	9.21%	14.84%

6.1.4. Branch: Uncooperative Peers Probability

In this last branch of simulations, we studied the effect of stressing the probability of uncooperative peers. The results in Table 12 show that, when the only stressed value is the probability of uncooperative peers (set to 10%), the network is operative. In this case, the probability of payment failure for uncooperative peers is 11.92%, but the probability of payment success remains above 50% (55.21%); the other probabilities of failure are almost the same as the non-stressing case.

Table 12. Simulation results of the branch of uncooperative peers probability.

Input Parameters				Output Measures			
r_π	σ_a	F_{sr}	$P_{\bar{c}_b}$	P_s	P_{f_r}	P_{f_b}	P_{f_e}
10	1	0.0%	0.0%	65.43%	24.40%	10.11%	0.0%
10	1	0.0%	10.0%	55.21%	24.31%	8.51%	11.92%
10	4	0.0%	10.0%	38.27%	46.10%	6.47%	9.13%

Again, to make sure that we did not miss non-operative cases, we stressed another parameter, the amount of payments (We did not stress the payment rate as we already showed that with 100 payments per second the network was non-operative and we did not stress the fraction of payments to the same recipient as we already studied this case (Section 6.1.3)). To stress the payment amount, we set σ_a to 4 (not to 5, the highest possible level of payment amounts in the variation interval because we already show in Section 6.1.1 that with this value the network is not operative). The results of this additional simulation shows that stressing together the probability of uncooperative peers and the payment amounts, the network is non-operative: the probability of success, in fact, is 38.27%. The probability of failure for uncooperative peers is 9.14% (similar to the case in which the only stressed value was $P_{\bar{c}_b}$). Instead, the main reason of the failures is the absence of viable routes (with a probability of 46.1%), due to the increased amounts of payments.

6.1.5. Discussion of the Main Findings

Payment amounts. When we set σ_a to 5, thus producing payments of the highest amounts (according to our interval and orders of magnitude, cf. Table 6), we discovered that the LN mainnet is non-operative, as the probability of success is only 46.13%. The main reason of the failure is the absence of viable payment routes, as the capacities of channels are not enough to forward payments of such amounts. While a naive solution would be to open channels with appropriate capacity, more elaborate approaches are beginning to appear, e.g., *Atomic Multi-Path Payments* [21], a technique that proposes to solve the payment amounts issue by splitting large payments into smaller ones which can be routed through channels with lower capacity, and then recomposed by the receiver.

Payment rate. Another non-operative case was found when we set the average payment rate to 100 payments per second. In this case, the probability of success was 43.88%. The main reason behind such a high failure rate is channel unbalancing: channel balances are depleted by an increased rate of payments to be forwarded. In addition, in this case, a naive solution would be to open channels with higher capacity, while a systemic alternative is represented by approaches akin to *REVIVE* [9], which allows channels to be re-balanced without the need of closing and re-opening them via on-chain transactions.

Uncooperative peers and payment amount. The last non-operative case resulted by the combination of a probability of uncooperative peers set to 10% and σ_a set to 4. In this case, the probability of payment success was 46.1%; payments most likely failed for absence of viable routes, due to the payment amounts, then with probability 9.14% payments failed for uncooperative behaviour of peers. Such results allows us to conclude the following: First, the probability of uncooperative peers, as long as limited to the realistic value of 10%, does not constitute a serious problem for the network. Second, we proved once again that increasing payment amounts is the most critical issue for the LN configuration taken into account; a few recently proposed countermeasures are briefly mentioned above.

6.2. Simulations on Synthetic Networks

This set of simulations studied the effect on performance of each independent variable, one at a time. The simulations were run on synthetic networks whose parameters (together with the parameters of the simulated payments) were defined by the independent variables of our study. For each independent variable, we ran more simulations, one for each value of the variable in the variation interval, while keeping the other variables set to their default values (cf. Table 5 for the variation intervals and Table 8 for the default values).

The results show that the simulated synthetic networks are generally characterised by good performance: in almost all cases, in fact, the probability of payment success was around 99%. In this section, we present and discuss the most relevant results; the detailed results of all simulations are available [online](#).

6.2.1. Channels Per Peer

In a decentralised network with 100 thousands peers, three channels per peer are not sufficient to have a robustly connected network. As shown in Table 13, with three channels, the probability of payment success is 59.61%; payments failed for absence of route (with probability 23.34%) and because the few existing channels were unbalanced (with probability 16.77%).

With five channels per peer, instead, performance is good: probability of success, in fact, is 99.34%. With 11 channels per peer, the optimal condition is reached, as the probabilities of payment failure for no route and for unbalancing are zero.

Table 13. Simulation results varying the number of channels per peer.

N_{ch}	P_s	P_{f_r}	P_{f_b}
3	59.61%	23.34%	16.77%
5	99.34%	0.31%	0.13%
8	99.82%	0.01%	0.0%
11	99.86%	0.0%	0.0%

6.2.2. Uncooperative Peers

As shown in Table 14, if the probability of uncooperative behaviour of peers is 10%, the probability of payment failure for uncooperative peers is 11.84%. When $P_{\bar{c}_b}$ is lower, the network performance is not significantly affected by uncooperative behaviour, as the probability of payment success is around 99%.

Table 14. Simulation results varying the uncooperative peers probability.

$P_{\bar{c}_b}$	P_s	P_{f_ε}
0.0%	99.36%	0.0%
0.01%	99.34%	0.0%
0.1%	99.27%	0.1%
1%	98.32%	1.04%
10%	87.47%	11.84%

6.2.3. Network Topology

The mean time to complete payments decreases as the network topology becomes more centralised. As shown by the results in Table 15, with one single hub (σ_t set to 0), mean payment time is 333.16 ms, while it grows to 1391.92 ms in a totally decentralised network with zero hubs (σ_t set to infinite). This is due to a corresponding decrease of the mean length of routes traversed by payments: with one single hub, almost each peer is connected to each other peer through the hub, so a route is on average long 2.90 hops, while it reaches 10.34 hops with zero hubs.

Table 15. Simulation results varying the network topology.

σ_t	P_s	T (ms)	L_r (hops)
0	99.88%	333.16	2.90
1	99.85%	536.83	4.13
10	99.83%	695.73	5.56
inf	99.34%	1391.92	10.34

However, also in a totally decentralised topology the synthetic HTLC payment network is characterised by good performance: the mean time to successfully complete payments, in fact, is approximately equal to 1.4 s, i.e., nearly instantaneous, and the probability of payment success is 99.34%.

6.2.4. Same-Recipient Payments

As shown in Table 16, when directing 50% of total payments (i.e., fifty thousands payments) to the same recipient, with a rate of 100 payments per second, the probability of failures for unbalancing reaches 16.06%. The reason is that channels direct to the destination peer unbalance, as they are traversed always in the same direction. Such unbalancing does not constitute a problem if fewer payments are directed to the same recipient: already with F_{sr} set to 40%, the probability of payment failure for unbalancing decreases to 0.1%.

Table 16. Simulation results varying the fraction of same-recipient payments.

F_{sr}	P_{fb}
0%	0.13%
10%	0.13%
20%	0.12%
40%	0.10%
50%	16.06%

6.2.5. Discussion of the Main Findings

We found that synthetic networks performed well: the probability of payment success, in fact, is close to 99% in almost all cases. We proved that the values of the network parameters used in this set of simulations (e.g., the average channel capacity and the number of channels per peer) are good candidates as ideal reference values that network participants should actively try to maintain in a distributed effort to keep the network in good health.

In a decentralised network with 100 thousands peers, where each peer has only three active channels, a payment succeeds with probability 59.61%, i.e., much less than the 99% that can be reached with five active channels per peer. Therefore, at least five channels per peer are needed to have a robustly connected network.

If a peer is uncooperative once every 10 times, the probability for a payment to fail due to such uncooperative behaviour is 11.83%. Hence, the probability of uncooperative peers (unless unrealistically high) does not constitute a serious issue in our synthetic networks.

Payment mean time for a totally decentralised topology is approximately 1.4 s, i.e., nearly instantaneous. As to be expected, the presence of well-connected hubs acting as payment gateways further reduces the payment mean time.

Thousands of payments directed toward the same recipient in a short time window determine the unbalancing of channels involved, especially those closer to the payee. Merchants who expect to receive a significant payment throughput should open many payment channels (more than the default five), to prevent payment losses.

7. Conclusions

The present research work focused on the Lightning Network, the mainstream proposal that aims to address the well-known scalability problem of the Bitcoin blockchain. Such solution implements an HTLC payment network, i.e., a network to securely route off-chain payments through HTLC contracts.

We developed CLoTH, a simulator of HTLC payment networks. The simulator takes as input: (i) parameters representing the HTLC network to be studied (e.g., peers, channels, and channel capacities); and (ii) parameters defining characteristics of the payments to be simulated on the HTLC network (e.g., payment rate and payment amounts). CLoTH simulates the defined payments script on the input network and produces performance measures in the form of payment-related statistics (e.g., the probability of payment failures and the mean time to complete a payment).

Since the LN protocol focuses on anti-censorship objectives and each node of the network is free to join and leave, it is difficult to anticipate unexplored configurations of an HTLC payment network and therefore to actuate those interventions that may guarantee network health (quick and successful payments). In this sense, CLoTH is a valid predicting tool to simulate possible troublesome configurations and to check in advance the effects of a routing optimisation action (e.g., a node that joins the network, and then establishes and funds several payment channels).

We ran simulations on a recent snapshot of the HTLC payment network of LN. We identified those configurations in which it is more likely for a payment to fail than to succeed, thus defining an operative limit for the network. We also proposed countermeasures to avoid the occurrence of such configurations and mentioned recently proposed counteracting approaches. The non-operative

configurations are a function of: payment amounts, payments rate, fraction of payments directed to the same recipient and the probability of uncooperative peers.

We also ran additional simulations on synthetic scenarios generated by statistical descriptions of HTLC networks and payment scripts. This second set of simulations aimed to separately study the impact on network performance of each individual CLoTH simulator input parameter. The results of these simulations show that the studied synthetic networks have good performance in most cases.

An analysis of the simulator execution led us to identify in the repeated local and inherently sequential application of the Dijkstra's algorithm the performance bottleneck of the simulator. In our future work, we will address this limitation by distributing the computation on a cluster of machines. Simulator performance improvement will allow us to perform additional experiments to complete the coverage of the parameter space and to experimentally prove HTLC protocol limitations, if any.

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Abbreviations

The following abbreviations are used in this manuscript:

LN Lightning Network
HTLC Hashed Timelock Contract

Appendix A. Reference Code Explanation

In this section, we describe the details of the 1nd code we took as reference to develop CLoTH. In 1nd, there are two main code structures which manage payments: *Switch* and *Link*. *Switch* is the messaging bus of HTLC messages: it is in charge of forwarding HTLCs or redirecting HTLCs initiated by the local peer to the proper functions. *Link* is the service which drives balance updates of a channel according to the HTLCs that concern the channel. In the following, we describe the functions included in the call graph in Figure 1.

- **SendPayment.** As shown by the numbers in the arrows, which represent the order of function calls, this function first tries to find possible routes to transfer the payment to the receiver and then tries to send the payment through one of the routes found. If the payment fails, it re-attempts the payment through one of the other viable routes found.
- **FindRoutes.** It attempts to find candidate routes which can route the payment to the receiver.
- **findPaths.** It runs the Yen's algorithm to find some paths to the payment receiver. A path is a set of channels which connect payment sender and payment receiver. In each internal iteration, to find a single path, it calls **findPath**. (We did not implement this function in CLoTH, as, in a recent version of 1nd, it has been replaced by the blacklist-based routing we described in Section 3).
- **findPath.** It runs the Dijkstra's algorithm, using timelock as distance metric. In fact, each channel endpoint has a *policy* which defines the timelock that will be applied to any HTLC established forwarded by that endpoint. The higher is this timelock in the endpoint policy, the higher is the distance.
- **newRoute.** It attempts to transform a path into a *route*. A route is a path which connects sender and receiver and which can also transfer the payment. A path is considered capable of transferring a payment if all channels in the path have a capacity greater than or equal to the payment amount, considering also fees. Fee is the amount of funds a channel endpoint withholds as a reward for forwarding a payment through that channel. In addition, fees are defined in the channel policy.

- **SendToSwitch.** It encodes the HTLCAdd message for the payment initiated and sends it to the first hop of the route, which is the local peer that initiated the payment.
- **SendHTLC.** It sends the HTLCAdd message to the Switch.
- **forward.** It directs an HTLC message to the proper function of the Switch.
- **handleLocalDispatch.** Function of the Switch that processes HTLCs relative to payments initiated by the local peer. If it receives an HTLCFail or HTLCFulfill message, which represent the result of a payment initiated by the local peer, it propagates back the result to SendPayment. If the payment failed due to changes in the topology (e.g., a channel that was closed), topology information of the local peer is updated. This function returns an error if there are no channels to the next hop with enough balance to forward the payment.
- **handlePacketForward.** Function of the Switch that processes HTLCs of payments initiated by other peers and to be forwarded by the local peer. It produces an HTLCFail if no channel to the next route hop has enough balance to forward the payment. The HTLCFail message is then sent back to the payment sender, as shown by the arrow with an empty dot.
- **HandleSwitchPacket.** It directs an HTLC from the Switch to the Link relative to the channel over which the payment will be forwarded.
- **handleDownStreamPkt.** Function of the Link which processes HTLCs coming from the Switch. It produces an HTLCFail if the channel does not have enough balance to forward the payment.
- **handleUpStreamMsg.** Function of the Link, the first called by a peer upon the reception of an HTLC message by another peer.
- **SendMessage.** Function to send over the network an HTLC message from a peer to another.
- **processLockedInHTLCs.** It processes an HTLC to decide whether to forward, fail or fulfill it. It returns an error if the local peer policy is not respected by the HTLC.
- **AddHTLC, SettleHTLC, ReceiveFailHTLC.** Functions called by handleUpStreamMsg or handleDownStreamPkt to update the local peer balance according to the HTLC received.

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